

1 Abstract

2 Many pathogens have clusters of variation in their genotypes that we refer to as strain structure. Importantly, when
3 considering related pathogen strains, host immunity to one strain is often neither independent from nor equivalent
4 to immunity to other strains. This partial cross-reactive immunity can thus allow repeated infection with (different
5 strains of) the same pathogen and shapes disease dynamics across a population, in turn influencing the effectiveness of
6 intervention strategies. To better understand the dynamics governing multi-strain pathogens in complex landscapes,
7 we combine two frameworks well-studied in their own right: multi-strain disease dynamics and metapopulation
8 network structure. We simulate the dynamics of a multi-strain disease on a network of populations connected by
9 migration and characterize the joint effects of disease model parametrization and network structure on these dynamics.
10 We find that the movement of (partially) immune individuals tends to have a larger impact than the movement of
11 infectious individuals, dampening infection dynamics in populations further along a chain. When disease parameters
12 differ between populations, we find that dynamics can propagate from one population to another, alternatively
13 stabilizing or destabilizing destination populations based on the dynamics of origin populations. In addition to
14 providing novel insights into the role of host movement on disease dynamics, this work provides a framework for
15 future predictive modelling of multi-strain diseases across generalized population structures.

16 1 Introduction

17 Many of the most impactful infectious diseases that affect humans (influenza, malaria, human
18 papillomavirus, *etc.*), livestock (porcine reproductive and respiratory syndrome, foot-and-mouth
19 disease, *etc.*), and wildlife (anthrax, plague, *etc.*) have clusters in their population-genetic variability
20 that we classify as strains. This variation in pathogen genotype is often associated with differences
21 in phenotype, which can have profound effects on the efficacy of host immune defenses. While the
22 human immune system is usually capable of preventing re-infection—*i.e.* infection with something
23 to which it has been previously exposed—sufficient, divergent evolution among pathogen strains can
24 reduce the ability of the host to recognize, and thus mount an immunological response to, subsequent
25 exposures. In some cases, this change is not sufficient to completely avoid recognition by the host’s
26 immune system, yielding an immune response that is neither as strong as it would be in the case

27 of re-exposure to the same strain, nor as weak as in the case of exposure to a novel pathogen.
28 This partial cross-reactive immunity can likewise lead to reduced transmissibility, affecting disease
29 dynamics across the population.

30 While the study of multi-strain diseases goes back decades (1; 2), the resulting modelling frame-
31 work has not yet been generalized to a collection of sub-populations connected through host move-
32 ment, *i.e.* a metapopulation (but see (3)). Initially introduced through the concepts of island
33 biogeography (4), the network approach of metapopulations can be applied to a variety of systems,
34 including human movement between cities, livestock transport between farms, and wildlife living
35 in fragmented natural habitats. In each case, there exist relatively high-density areas which are
36 connected to one another through a network of individuals' movement. A metapopulation frame-
37 work allows the application of network analyses to characterize patterns of connection within the
38 larger system, and can provide unique insights across scales.

39 Historically, metapopulation studies have been divided into two main camps: those that mo-
40 del within-population dynamics and “cell occupancy” models. The latter of which, where only the
41 presence or absence of a given species within a population is recorded in a given timepoint (5), has
42 received much more theoretical attention. Importantly, cell occupancy models rest on an assump-
43 tion of temporal separation in which local dynamics occur on a timescale that can be treated as
44 instantaneous relative to that of the between-population dynamics (6). When considering patho-
45 gens in systems with relatively high migration rates, however, this assumption rarely holds, and the
46 presence-absence approach can significantly limit model accuracy (7; 8; 9).

47 The presence of metapopulation structure has been repeatedly associated with increased stabili-
48 ty (10; 11; 12). This is due in part to the ability of migration between asynchronous populations to
49 rescue temporarily low density populations from extinction (13). This is particularly relevant when
50 populations are undergoing cyclical or chaotic dynamics, where repeated instances of low density
51 are generally considered to be at greater risk of extinction than a population maintaining steady
52 state dynamics (14; 15).

53 Here, we build on the strain theory of host-pathogen systems proposed by (16), considering a scenario

54 where a collection of populations undergoing local dynamics are furthermore interconnected through
55 the movement of individuals between populations. We simulate disease dynamics on this system,
56 characterizing the effects of parametrization and network structure on these dynamics. This work is
57 divided into three sections: first, we explore a case of interconnected populations which have been
58 parametrized to display identical dynamics in the absence of host migration. Second, we consider
59 cases where parameters differ between populations. Finally, we explore the role of network structure
60 on disease dynamics in larger networks of connected populations.

61 2 Methods

62 2.1 Model framework for one population

63 We work from a system of ordinary differential equations which delineate a population into classes
64 based on current and past exposure to different strains of a pathogen. Pathogens with strain struc-
65 ture can differ in both the number of strains and the level of cross-reactive immunity afforded by
66 past exposure to similar strains. To model the number of strains, we signify a strain $i = \{x_1, x_2, \dots,$
67 $x_n\}$ as a set of n loci, each of which can take on a finite number of alleles. For instance, a pathogen
68 with two loci (a and b) and two alleles at each loci has a total of four potential strains: $\{a_1, b_1\}$,
69 $\{a_1, b_2\}$, $\{a_2, b_1\}$, $\{a_2, b_2\}$. For cross-reactive immunity, we use a parameter γ which indicates the
70 degree of reduced susceptibility a host has to strains that are similar to (*i.e.* strains that share
71 at least one allele with one another) past exposures. Importantly, in this framework, the number
72 of strains is fixed and finite. While strains may go extinct over time, there is no process for the
73 generation of new strains or to re-introduce strains that had previously gone extinct (but see (16)).

74 The model consists of sets of three nested equations (one set for each strain i): y , z , and w . See (17)
75 for a more comprehensive discussion of the model framework, including a graphical representation.
76 y_i represents the proportion of the population currently infectious with strain i . z_i represents the
77 proportion of the population that has been exposed to strain i . These individuals harbor complete
78 immunity to future infections with strain i and include those currently infected, *i.e.* y_i , those that
79 have recovered but were previously infectious, and those that were exposed, but protected from

80 becoming infectious due to partial cross-protective immunity. Finally, w_i represents the proportion
81 of the population which has been exposed to any strain j which has at least one allele in common
82 with strain i (including strain i itself), *i.e.* $j \cap i \neq \emptyset$. These individuals have at least partial
83 immunity to strain i . *N.b.* these equations are nested such that any individual in y_i is also in z_i and
84 any individual in z_i is also in w_i , and $y_i \leq z_i \leq w_i \forall$ strain i . In traditional Susceptible-Infected
85 (SI), Susceptible-Infected-Recovered (SIR), *etc.* single-strain mathematical frameworks: the y class
86 is analogous to the I class, while w and z are composed of combinations of I and R classes. The
87 susceptible population is not modelled explicitly in this framework.

88 Explicitly, these three equations (for a given strain i) are:

$$\begin{aligned}
\frac{dy_i}{dt} &= \beta ((1 - w_i) + (1 - \gamma)(w_i - z_i)) y_i - \sigma y_i - \mu y_i \\
\frac{dz_i}{dt} &= \beta (1 - z_i) y_i - \mu z_i \\
\frac{dw_i}{dt} &= \beta (1 - w_i) \sum_{j \ni j \cap i \neq \emptyset} y_j - \mu w_i
\end{aligned} \tag{1}$$

89 As above, we denote strains as subscripts and, in the equation for w_i , we sum over all strains j which
90 share at least one allele with the focal strain i . β , σ , and μ are the infection, recovery, and death
91 rates, respectively. γ (as mentioned above) is an indicator of the level of cross-reactive immunity
92 gained by prior exposure to alleles in the target strain. Note that while we depict only one value per
93 demographic parameter (*i.e.* all strains are functionally equivalent) for clarity of notation, these
94 values could also be written to vary by strain (*e.g.* β_i).

95 Immunity in this framework is non-waning: exposure to a strain yields consistent protection from
96 future infection over the lifespan of the individual. Moreover, this protection is trichotomous: an
97 individual can either have no protection from a given strain (it has not seen any of the alleles
98 before), complete protection (it has seen this exact combination of alleles before), or a set point
99 in-between according to the parameter γ (it has seen at least one, but not all alleles before). Put
100 another way, we do not distinguish between loci, assuming that sharing an allele at one locus is
101 functionally identical to sharing an allele at any other locus, or indeed all other loci except one.

102 **2.2 Extensions to more than one population**

103 Following (18), we model movement between populations using a dispersal matrix $\Delta = \mathbf{A} - \mathbf{E}$,
 104 where \mathbf{A} is the weighted adjacency matrix containing elements A_{kl} indicating the proportion of
 105 population k (row) moving to population l (column) per unit time and \mathbf{E} is a diagonal matrix
 106 representing emigration, where each entry $E_{kk} = \sum_{k=1}^n A_{kl}$ where n is the number of populations.
 107 Thus, the whole system can be depicted by a set of three equations per strain i per population k :

$$\begin{aligned}
 \frac{dy_{i,l}}{dt} &= \beta((1 - w_{i,k}) + (1 - \gamma)(w_{i,k} - z_{i,k})) y_{i,k} - \sigma y_{i,k} - \mu y_{i,k} + \sum_k \Delta_{kl} y_{i,k} \\
 \frac{dz_{i,l}}{dt} &= \beta(1 - z_{i,k}) y_{i,k} - \mu z_{i,k} + \sum_k \Delta_{kl} z_{i,k} \\
 \frac{dw_{i,l}}{dt} &= \beta(1 - w_{i,k}) \sum_{j \ni j \cap i \neq \emptyset} y_{j,k} - \mu w_{i,k} + \sum_k \Delta_{kl} w_{i,k}
 \end{aligned} \tag{2}$$

108 Where Δ^T signifies the transpose of Δ , and each equation from Section 2.1 is now additionally
 109 indexed according to population and has an additional term to account for migration between
 110 populations. While in principle the elements of Δ can take any value $[0, 1]$, signifying a (continuous)
 111 movement of between 0 and 100% of individuals, for simplicity we use a constant value δ for the
 112 strength of each movement, *i.e.* for each non-zero off-diagonal element of Δ . Sensitivity to this
 113 value is explored in the supporting information (Fig S2).

114 This framework can be applied to a metapopulation of arbitrary size and complexity, with the
 115 number of equations being linearly related to the number of populations. The dynamics of each
 116 population are governed by a set of three equations per pathogen strain, and these equations
 117 are interlinked within populations by partial, cross-reactive immunity, and between populations
 118 through a movement network. The total number of differential equations for any given system will
 119 be three times the number of strains multiplied by the number of populations in the metapopulation.

120 **2.3 Simulation Procedure**

All simulations were carried out in Julia version 1.3.0 (19), with graphics produced using the ggplot2
 package (20) in R version 3.6.1 (21). For simplicity of presentation, we fix the values of all variables

other than β (the infection rate) and Δ (the network of movement information) to be identical for all populations in the metapopulation. To demonstrate the variety of dynamics obtainable in this modeling framework, we vary

$$\tilde{R}_0 = \frac{\beta}{\sigma + \mu + E_{kk}},$$

121 where $E_{kk} = -\Delta_{kk}$, as noted above, signifies the total outgoing movement from the population of
 122 interest. We add a \sim over R_0 to denote that this is an approximation of the true reproductive
 123 number, the precise form of which would additionally take into account the inflow of infectious
 124 individuals from other populations. We additionally vary Δ according to the number and inter-
 125 connectedness of the populations. For the figures of the main text, we utilize a strain structure of
 126 two loci, each with two alleles. Sensitivity to these parameter choices is explored in the supporting
 127 information (Fig S3).

128 **2.3.1 Populations with identical parametrizations**

129 To assess the effect of migration on population dynamics, we first consider the simplest case of a
 130 set of populations sharing the same disease parametrization: β such that $\tilde{R}_0 = 2$, $\sigma = 8$, $\mu = 0.1$,
 131 and $\gamma = 0.66$. We use a movement network described by a chain of populations, *i.e.* $A \rightarrow B \rightarrow C \rightarrow D$
 132 or

$$\Delta = \begin{bmatrix} -\delta & \delta & 0 & 0 \\ 0 & -\delta & \delta & 0 \\ 0 & 0 & -\delta & \delta \\ 0 & 0 & 0 & 0 \end{bmatrix},$$

133 where $\delta = 0.05$, and ask how the dynamics of populations further down the chain (*i.e.* B, C, D)
 134 differ from those of the origin population (*i.e.* A), recalling that, without migration, all populations
 135 would have identical dynamics.

136 **2.3.2 Populations with varying parametrizations**

137 We next consider the case where parameters differ between connected populations, we restrict our
 138 consideration to a system of two populations, identical in all respects other than the parameter β ,

139 which is set to either induce a steady state of coexisting strains (β such that $\tilde{R}_0 = 5$ in population
 140 A) or cyclically coexisting strains (β such that $\tilde{R}_0 = 2$ in population B). We then display three
 141 potential patterns of connection: no migration (left column), A \rightarrow B (middle column), and B \rightarrow A
 142 (right column). Specifically, we set

$$\Delta = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}, \Delta = \begin{bmatrix} -\delta & \delta \\ 0 & 0 \end{bmatrix}, \text{ and } \Delta = \begin{bmatrix} 0 & 0 \\ \delta & -\delta \end{bmatrix},$$

143 respectively, again with $\delta = 0.05$, $\sigma = 8$, $\mu = 0.1$, and $\gamma = 0.66$.

144 To address the case of multiple origin populations feeding into a single destination population, we
 145 consider a system of three populations: A \rightarrow C \leftarrow B, or

$$\Delta = \begin{bmatrix} -\delta & 0 & \delta \\ 0 & -\delta & \delta \\ 0 & 0 & -\delta \end{bmatrix},$$

146 where populations A and C have β corresponding to an $\tilde{R}_0 = 5$, but population B has β correspond-
 147 ing to an $\tilde{R}_0 = 2$; all other parameters as above.

148 **2.3.3 Larger network structure**

149 Finally, we characterize the role of global network structure through considering the impact of
 150 degree distribution on a few summary statistics of system-wide disease burden: the mean proportion
 151 of infectious individuals (area under the currently infectious (*i.e.* y) curve), the mean level of strain-
 152 specific immunity (average z value), and the mean time between epidemic peaks (*i.e.* between local
 153 maxima in y) over the course of the final 33% of the simulation. We omit the initial period of the
 154 simulation to reduce the impact of transient dynamics.

155 We perform 100 simulations for each of five generic network ensembles each with 25 populations
 156 and a connectedness of approximately 0.15. Specifically, we examine Erdős-Rényi (links randomly
 157 assigned between populations), stochastic block (a metapopulation consisting of two groups of po-

158 pulations which have high migration within the group, but low migration to populations in the other
159 group), tree-like (where there are many chains of populations and no potential for cycles), Barabasi-
160 Albert (a scale-free network in which there tends to be a few populations with very many links,
161 and many populations with few links), and Watts-Strogatz (a small-world network structure which
162 is produced by partially re-wiring a spatially connected grid of populations) network structures. To
163 generate these networks, we utilize functions from the tidygraph R package (22), except in the case
164 of the tree and Watts-Strogatz configuration for which we use custom algorithms. Note that we use
165 a parameter of attachment of 4 for the Barabasi-Albert random graphs. This allows for comparable
166 connectences to the other random graphs as well as distinguishing these randomizations from trees
167 (as would result from a default parameter of attachment of 1). In all cases, each migration strength
168 is set to a constant $\delta = 0.01$, only the pattern of connections varies. Each population is assigned
169 a random β value corresponding to a \tilde{R}_0 between [1, 6]. These results are qualitatively similar if
170 instead every population is assigned the same value of β .

171 All code is made available on GitHub: <https://git.io/JeqMc>.

172 **3 Results**

173 In the following sections, we provide figures to demonstrate the effect of metapopulation structure on
174 disease dynamics. In these figures, we plot a time series for each of three subsets of the population:
175 those currently infected with a particular strain of the pathogen, those having (complete) specific
176 immunity against the focal strain, and those who have at least partial cross-reactive immunity to
177 the focal strain, due to past exposure to a similar strain (see Methods). Populations differ in their β
178 (and thus R_0) value. This can be considered, for example, as differences in population density, which
179 affects the probability of disease transmission. We only depict one representative strain in each
180 plot for visual clarity and parametrize the model such that all strains are functionally equivalent
181 (*i.e.* they all have the same transmission and recovery rates within any given population).

182 **3.1 Cyclical dynamics are dampened along chains in the metapopulation net-** 183 **work**

184 We found that even when all populations share the same parametrizations and initial conditions,
185 that populations further along network chains have reduced proportions of currently infectious
186 individuals and dampened oscillatory dynamics compared to those they would exhibit in isolation
187 (Fig 1). This is due to the movement of (partially) immune individuals between the populations,
188 increasing the proportion of individuals with specific and cross-reactively immunity in populations
189 further along the chain. While infectious individuals move at an equal rate, the proportion of the
190 population that is currently infectious at any given time is much smaller than the proportion with
191 immunity.

192 **3.2 Dynamics propagate through metapopulation networks**

193 We found that in the case of a simple chain of populations, the dynamics of destination populations
194 can be overridden by the dynamics of origin populations (Fig 2). Interestingly, this is true both
195 of cyclical dynamics overruling stable dynamics and *vice versa*, though the required amount of
196 migration differs according to the origin and destination dynamics (see supporting information
197 Fig S2). This migration can also allow for strain coexistence even in populations where the local
198 parameters would suggest extinction of one or more strains.

199 The issue of dynamics propagation gets more complicated when there are multiple, varying origin
200 populations for a given destination population. We found that there is a hierarchy of dynamics in
201 their propagation through the network: when there are origin populations with both cyclical and
202 steady state dynamics, the destination population inherits the cyclical dynamics (Fig 3), albeit
203 dampened from what they would have been without migration from a steady state population.
204 This asymmetrical inheritance is robust to imbalance in the relative contributions of the origins. Put
205 another way, if just one of many origin populations (or a small proportion of the total movement)
206 has cyclical dynamics, the destination population will also have cyclical dynamics.

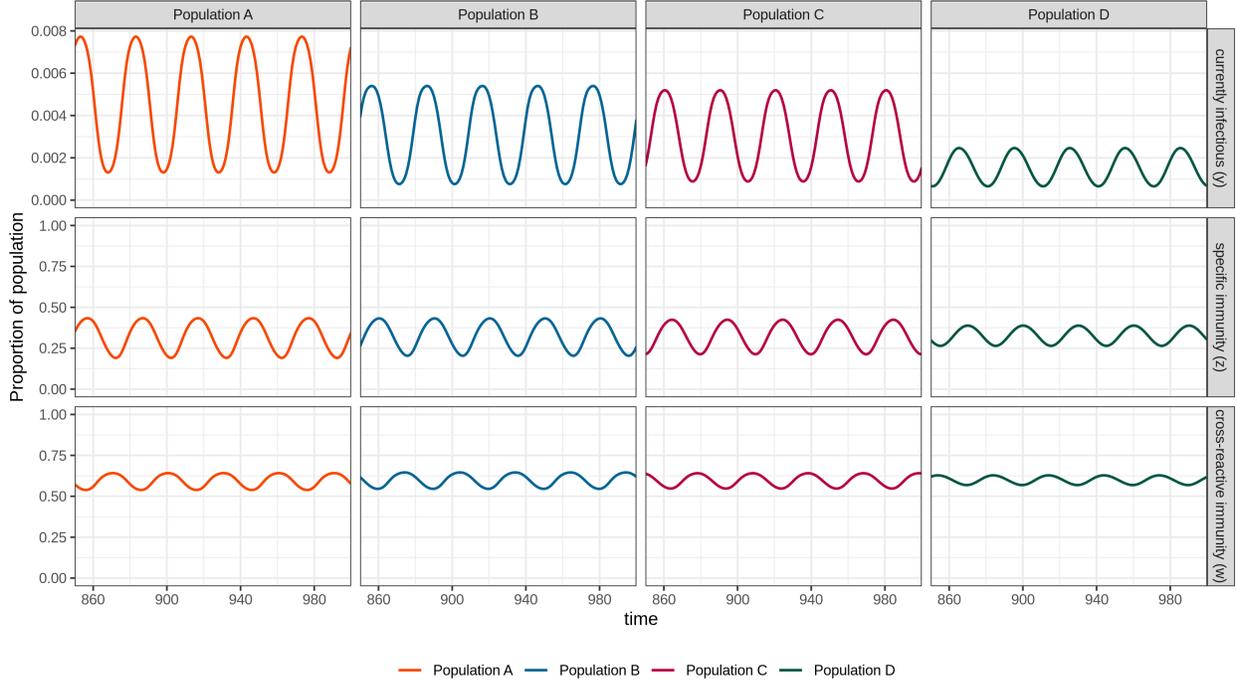


Figure 1: Connecting multiple populations with the same parameters results in reduced pathogen prevalence and dampened cycles in populations further down the chain. Here, populations are connected such that $A \rightarrow B \rightarrow C \rightarrow D$. Each column indicates a population, while each row is one of the three population classes laid out above and in the Methods, *i.e.* those currently infectious with the given strain, those with (complete) specific immunity to the given strain, and those with partial cross-protective immunity to the given strain. The mean level of immunity (both specific (middle row) and cross-reactive (bottom row)) increases in each sequential population, while the mean level of currently infectious individuals (top row) decreases. All populations have parameters $\sigma = 8$, $\mu = 0.1$, $\delta = 0.05$, $\gamma = 0.66$ and a β chosen to make $\tilde{R}_0 = 2$ for all populations. We use a two-loci, two-allele strain structure, but show only one strain for clarity (but see supporting information Fig S1).

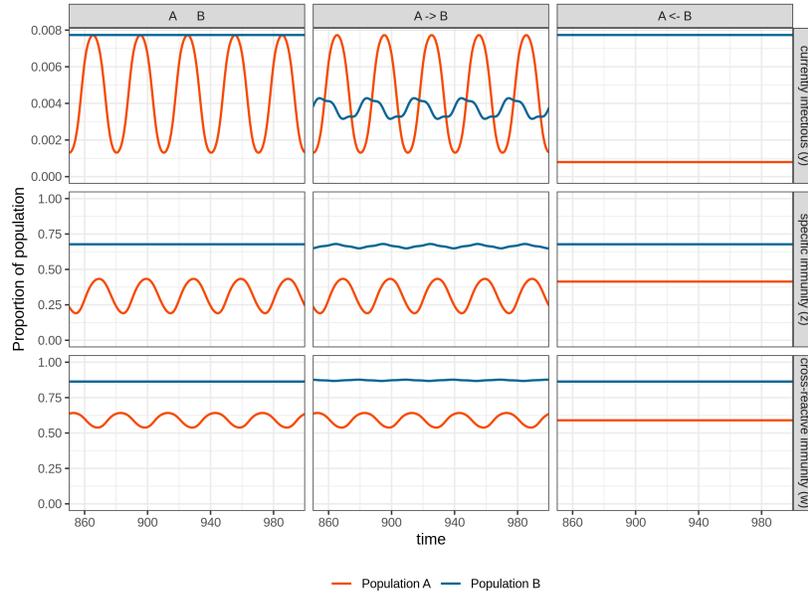


Figure 2: Destination populations tend to inherit origin population dynamics when linking populations with different model parametrizations. As in Fig 1, rows correspond to population classes, but here, columns indicate network structure. While in isolation (left column), population A has cyclical dynamics and population B has steady-state dynamics, when the two populations are linked by migration, the destination population inherits the dynamics of the origin population (center and right columns). This is true regardless of the direction of the movement (depending on the level of migration; see supporting information Fig S2). Populations A and B have parameters $\sigma = 8$, $\mu = 0.1$, $\delta = 0.05$, and $\gamma = 0.66$ in common and β chosen to reflect $\tilde{R}_0 = 2$ and 5, respectively. We use a two-loci, two-allele strain structure, but show only one strain for clarity.

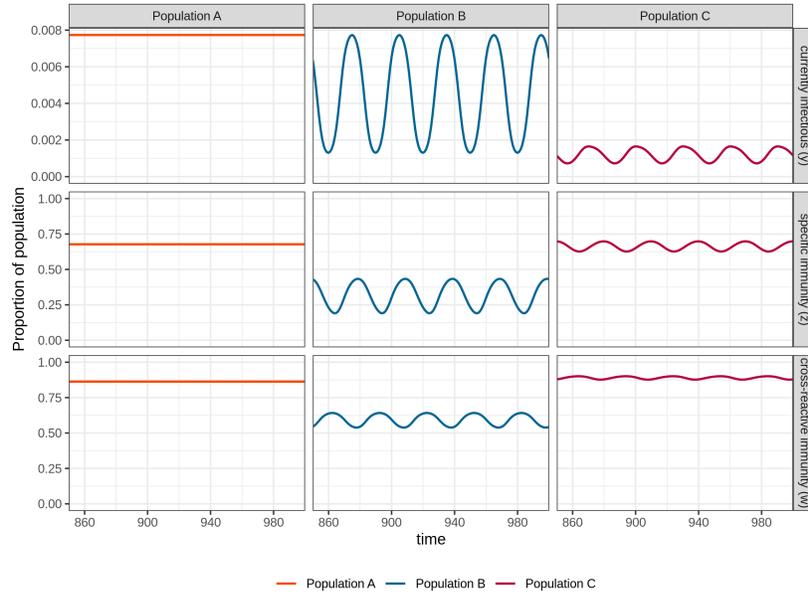


Figure 3: When multiple origin populations differ in their dynamics, the destination population inherits cycles over steady states. As in Fig 1, rows indicate population classes, and columns the component populations. Here, we have populations A and B feeding into population C at the same rate of $\delta = 0.05$. Populations A and C are parametrized to produce steady state dynamics in the absence of migration, with $\sigma = 8$, $\mu = 0.1$, $\gamma = 0.66$, and β corresponding to a $\tilde{R}_0 = 2$. Population B shows cyclical dynamics with β corresponding to a $\tilde{R}_0 = 5$ and all other parameters the same. Note that, even though the parameters of population C would lead to a steady state in the absence of migration, we see cyclical dynamics being inherited from population B. We use a two-loci, two-allele strain structure, but show only one strain for clarity.

207 **3.3 Degree distribution affects pathogen prevalence and immunity**

208 These simple patterns in the effects of origin population dynamics on those in the destination popu-
209 lation have clear implications when pieced together into larger network structures. For instance, the
210 propagation of immune individuals through the metapopulation suggests that populations further
211 “up the chain” will tend to have higher on-average disease incidence and also greater variability.
212 The inheritance of dynamical regimes combined with a hierarchy of dynamics in that inheritance
213 suggests that chaos and cycles should be more common, especially in populations further “down
214 the chain.” That is, except in cases where the ultimate origin populations are all disposed toward
215 steady states, in which case the stabilizing effect could overrule downstream local parametrizations,
216 leading to an overall stable system.

217 In Fig 4, we report the effect of various network structures on three summary statistics of pathogen
218 prevalence (and levels of immunity) using five common network ensembles. Depending on the
219 system being explored, empirical network structures might have elements in common with one or
220 more of these ensembles, for instance, many social networks are considered to be “small-world” in
221 structure like Watts-Strogatz random graphs, while ecological networks are often commented on
222 for their formation of “modules” or clusters of more densely interacting species as in stochastic
223 block random graphs. Networks were parametrized to have approximately equal connectance and
224 size in order to reduce uninformative variation (see Section 2.3.3). This is because metapopulation
225 size and connectance have known effects on pathogen persistence, independent of further network
226 structure (23; 24; 25).

227 We found that the network configurations with higher variation in indegree (*i.e.* the number of
228 other populations each population receives migration from) distributions (supporting information
229 Fig S4), such as those found in the tree and Barabasi-Albert networks, tend to have higher levels
230 of infection over time, despite similar levels of immunity as the other three network types. We
231 saw similar patterns to those in infectious individuals when looking at time between epidemic
232 peaks across network types. While fewer of the populations ended up with cyclical dynamics in the
233 Barabasi-Albert graphs, the mean period of the cycles tended to be slightly higher and have higher

variance, but this was not robust to alternative parametrizations (supporting information Fig S5).

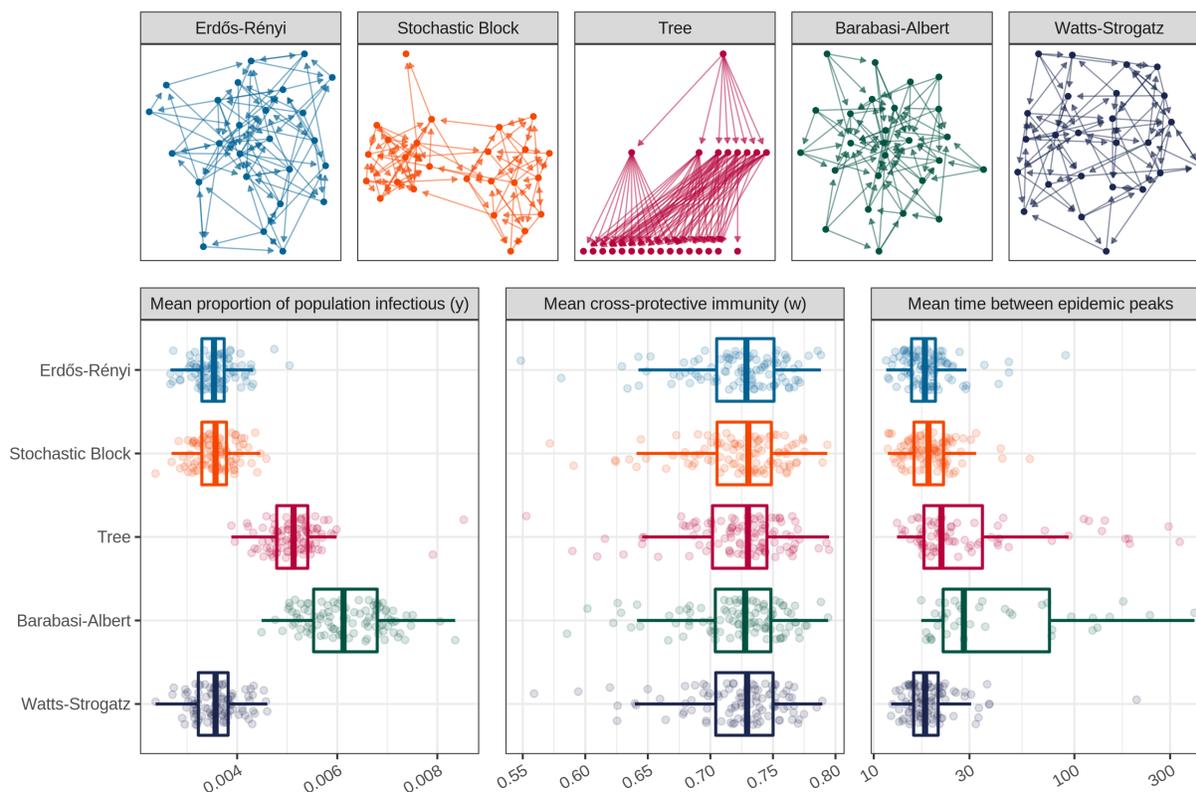


Figure 4: The effect of network structure on pathogen prevalence and levels of immunity through time. In the top row, we depict a representative network from each of the five ensembles. The second row shows the distributions of each of three response variables for prevalence of the pathogen and specific immunity over the course of the simulation, with the units for the horizontal axes given by the panel headings. We depict one point for each randomized network structure and box-plots indicating the median and inter-quartile range of each network-type’s distribution. Network generating algorithms were tuned to produce networks of the same size and approximate connectance and model parameters were either the same for all populations and across simulations ($\sigma = 8$, $\mu = 0.05$, $\delta = 0.01$, and $\gamma = 0.66$) or randomized for each population in each simulation (initial densities of infectious individuals $[0, 1]$ and β value corresponding to a \tilde{R}_0 within $[1, 6]$ for each population).

234

235 4 Discussion

236 Both metapopulation (26) and strain (16) structure have long been known to be important to
 237 disease dynamics and are increasingly being recognized as ubiquitous. Yet the combination of
 238 these two areas of theory has been underexplored. We show here that this lacuna can have real

239 consequences for our understanding of disease dynamics in empirical systems.

240 In probing the relationship between origin and destination dynamics in simple metapopulations,
241 we have demonstrated several patterns that expand our understanding of disease dynamics in
242 these systems. By directly incorporating a movement network into our model framework, we have
243 constructed a very general approach that lends itself to arbitrarily large and complex systems.
244 This is noteworthy, as more and more natural systems are being thought of in terms of networks
245 of interacting components (*e.g.* separate species in ecological communities (27) or host individuals
246 exchanging parasites (28)). By adjusting the scale of our metapopulation, we can ask and answer
247 different questions about the forces influencing disease dynamics.

248 We found that the dynamics of prevalence and immunity among migrationally connected popu-
249 lations are not independent, and that even very small rates of population movement can have
250 profound effects on a population’s disease dynamics: from reducing pathogen prevalence to chang-
251 ing the dynamical regime of destination populations entirely. Our findings regarding the reduction
252 in cycle amplitude (Section 3.1) echo results in dispersal networks in ecology, where population
253 dynamics were dampened following the introduction of migration (29).

254 Contrary to prior focus in the literature on the role of migrating infectious individuals (30; 31;
255 26), we found that the migration of immune individuals can be equally (or even more) important.
256 This is noteworthy, as the few previous studies relating multi-strain diseases and metapopulation
257 structure only allow pathogen transmission between populations, not the movement of individuals
258 explicitly (3; 32)—an approach that is more mathematically tractable, but omits the potentially
259 influential transmission of immune individuals.

260 Finally, we show that larger network structure also has a part to play in disease dynamics, resulting
261 in significant differences in pathogen prevalence across network types. Our results are in agreement
262 with previous results suggesting increased epidemic size in scale-free network structures (such as
263 those found in Barabasi-Albert random graphs) when the spreading rate is sufficiently slow (33;
264 34) due to the high-degree nodes serving as “super-spreaders” (35; 25). Along these lines, there
265 has been some previous research indicating that node degree (the number of other populations a

266 given population is connected to) is directly related to pathogen prevalence in that focal population
267 ((36), but see (37)), however a complete investigation into network structure at the node-level is
268 beyond the scope of this work. A comprehensive investigation of the role of more complex network
269 structures in disease dynamics, however, remains a topic for further investigation.

270 In this work, we have utilized a relatively simple model for disease dynamics in an effort to maximize
271 interpretability. Such simplification inevitably comes with a cost, and several of our assumptions
272 can be critiqued as unrealistic. Perhaps foremost is the assumption of continuous movement. While
273 continuous movement might be appropriate for very large populations with frequent, relatively
274 small migrations between them, when any of these three components is not present, we would expect
275 deviation from these predictions. Future work could explore the importance of discrete movement
276 regimes on these patterns. Likewise, in this work we omit strain mutation and recombination (17)
277 (yet the latter is included in the original framework of (16)). The generation of novel strains is
278 likely important to the global persistence of diseases in humans (38) and animals (39). Finally,
279 in representing movement by adding a proportion of the origin population to the destination, we
280 introduce an assumption that the two populations in question are of approximately the same size.
281 In a metapopulation where populations vary widely in size, the proportion leaving one population
282 would not correspond to the proportion entering another.

283 This work should not be seen as an attempt at comprehensive categorization of the role of meta-
284 population structure on the dynamics of multi-strain diseases, but rather as an initial step in
285 exploring the complex interplay between the population structure of hosts and strain structure of
286 pathogens. Our results suggest there may be simple rules underlying this relationship, at least for
287 a wide range of parameter values, but it remains to be seen where networks based on empirical
288 data fall in these parameter regimes, as well as how such systems might deviate from theoretical
289 expectations.

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375 **S1 Supporting Information**

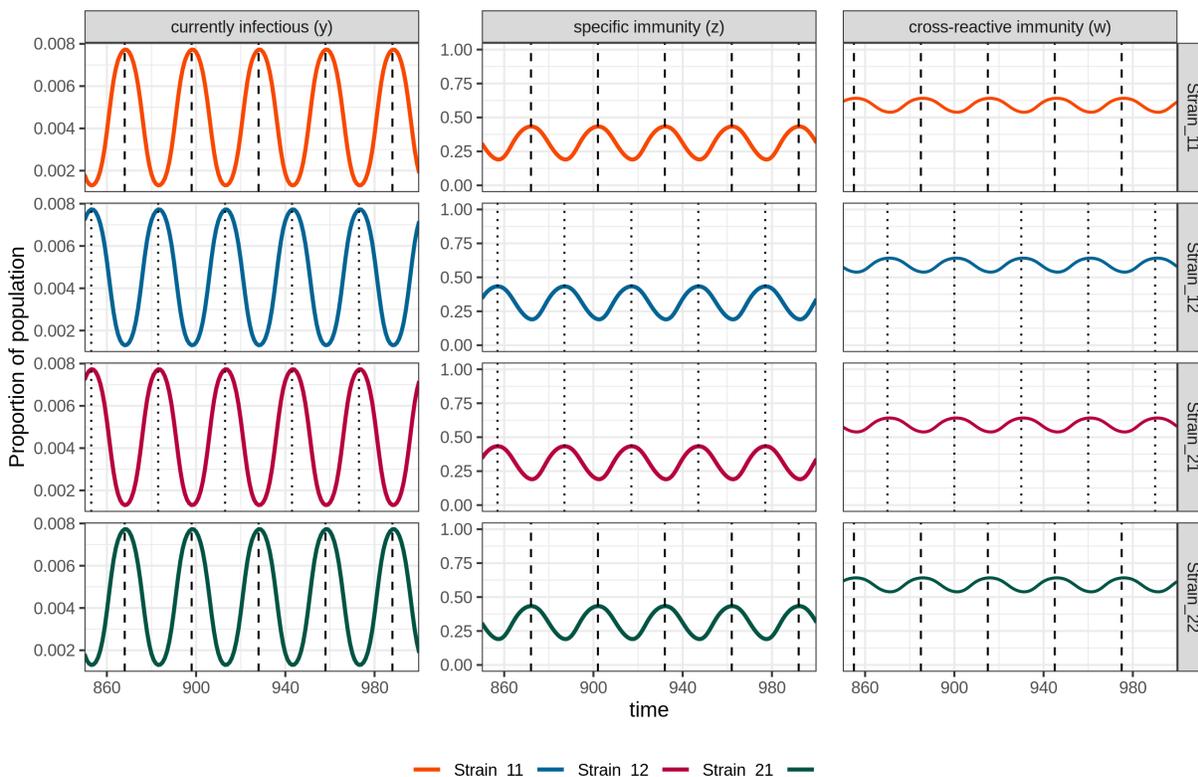


Figure S1: Considering all the dynamics of all four strains from population A in Fig 1. Note that lines are colored according to strain rather than population. Strains can be divided into two discordant sets of non-overlapping alleles: $\{1, 1\}$ and $\{2, 2\}$, and $\{1, 2\}$ and $\{2, 1\}$. Each strain of a discordant set behaves identically due to identical parametrization and no interaction between strains that do not share at least one allele, but discordant sets interact with one another due to partial cross-reactive immunity. Thus, when one set is abundant, the other is rare and *vice versa*. We highlight the maximum value of each discordant set's cycle with a vertical line in order to facilitate comparisons between strains and sets.

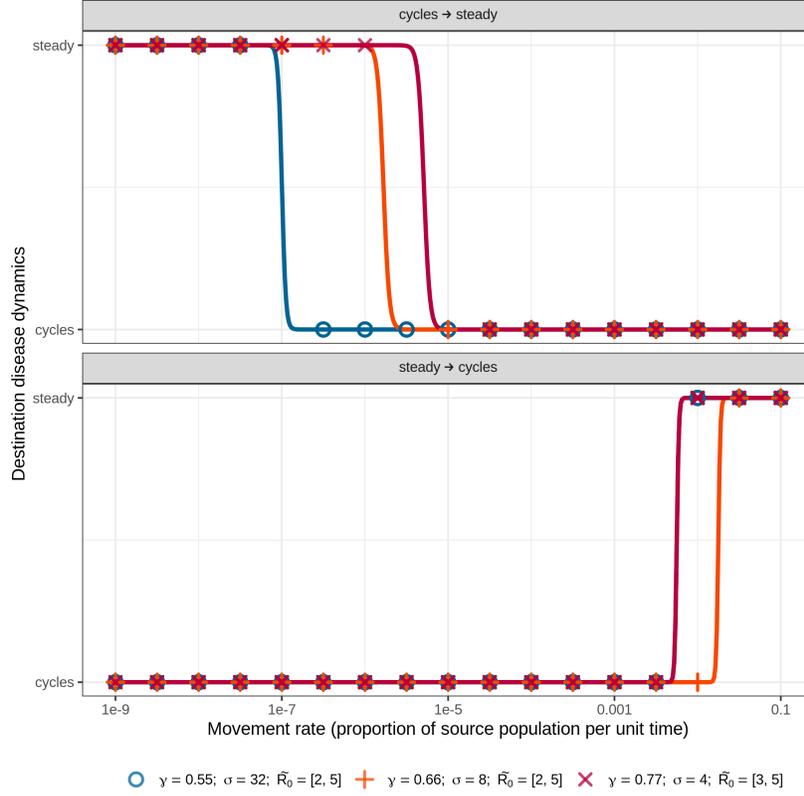


Figure S2: The effect of variable migration rate on transference of dynamical regime from origin to destination in a simple metapopulation of two populations linked by unidirectional movement. In the top panel are cases where the origin population has cyclical dynamics and the destination has steady state dynamics when in isolation, while in the bottom panel the opposite is true. As the movement rate (δ : horizontal axis) increases, there is a phase-transition at which point the destination population's dynamics (indicated by the vertical axis) switch to match those of the origin. We fit a binomial spline to highlight this transition point. We see that even with very small rates of migration, a stable population can be converted to a cyclical one (top panel). Yet, it is more difficult to convert a cyclical population to one with steady state dynamics (bottom panel). Three parametrizations are recorded here (color; see legend), with additional parameter $\mu = 0.15$ being the same for both populations. Finally, note that the two values of \tilde{R}_0 listed in the legend correspond to the two populations, with the larger value corresponding to the steady state population and the smaller value the cyclical population (when in isolation) .

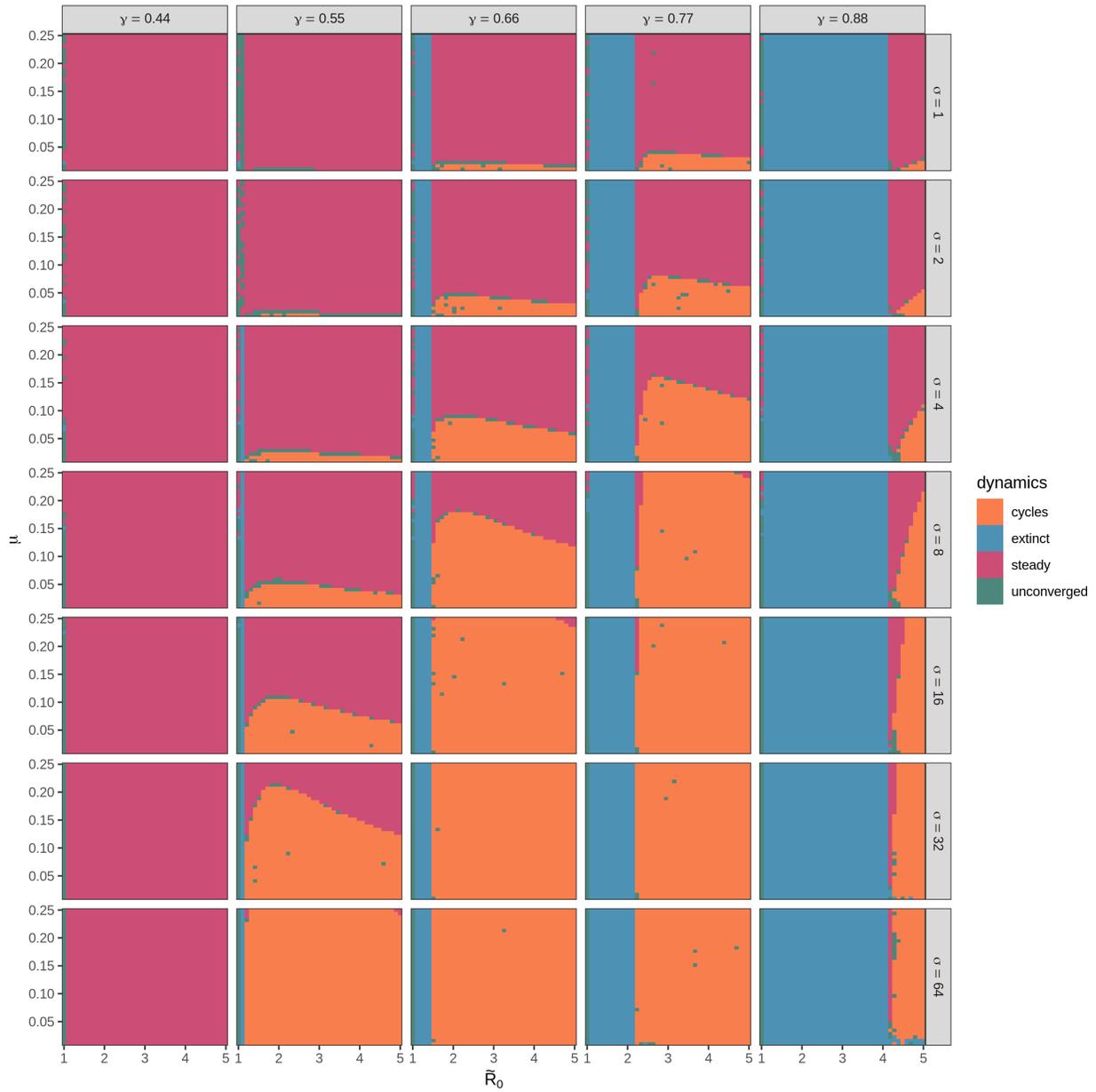


Figure S3: Effect of parametrization on dynamic regime for a population in isolation. Here, columns indicate values of γ and rows indicate values of σ . Depending on the combination of β , σ , μ , and γ , a population can exhibit a range of dynamics including steady states for all strains (pink), cyclical or chaotic dynamics for all strains (orange), or partial extinction of some strains (blue). Green cells indicate a numerical failure in integration. All simulations here utilize a two-loci, two-allele strain structure. See (16) for a similar figure for alternative parameterizations.

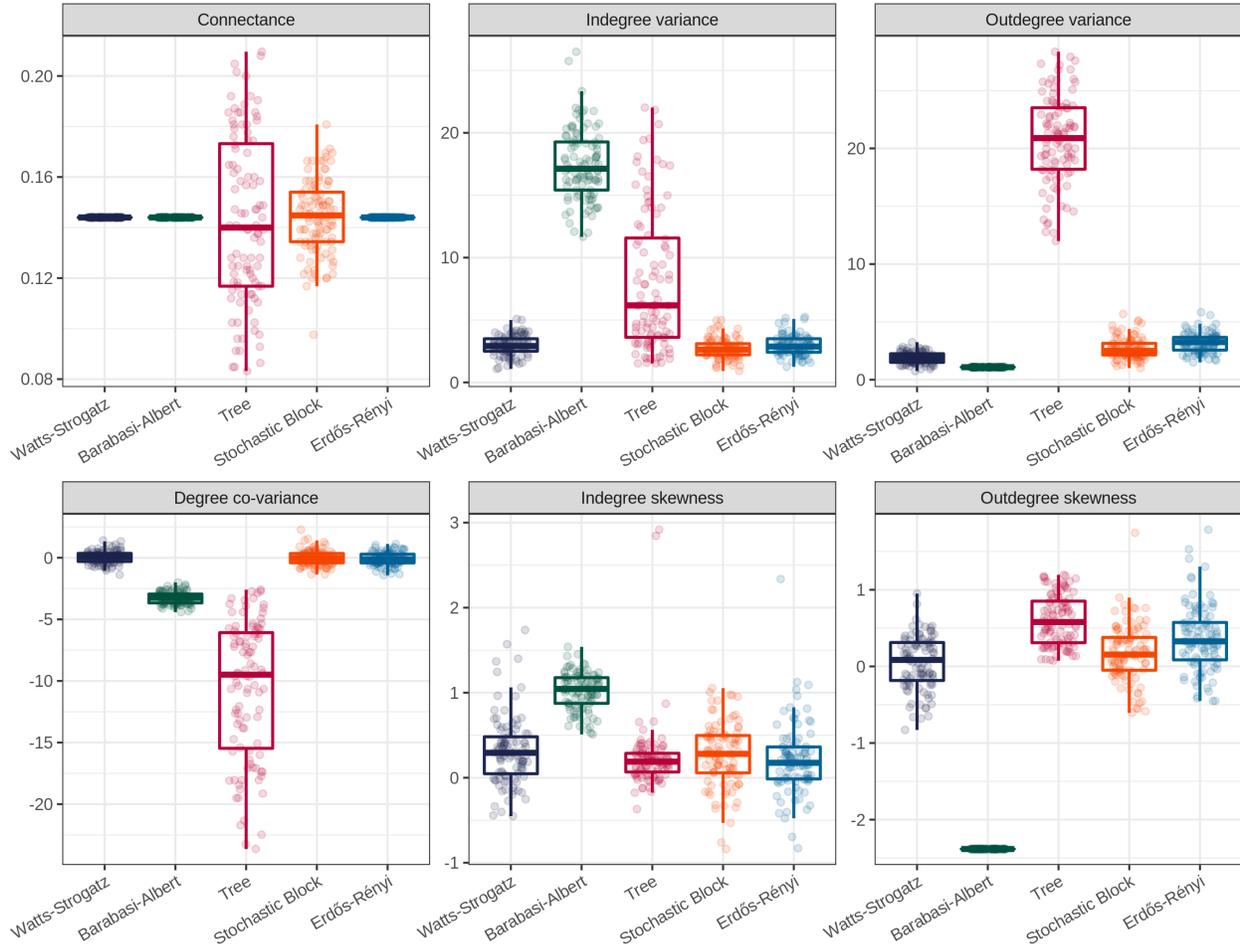


Figure S4: Summary statistics for the degree distributions of each randomized network used for Fig 4 in the main text. Networks were constructed to have the same size and approximate connectance, but with the network structure (which populations are connected to which other populations) otherwise generated according to one of five algorithms: Erdős-Rényi, Barabasi-Albert, and Watts-Strogatz, stochastic block, and tree (see Section 2.3.3 of the main text). Some algorithms allowed perfect matching of connectance (Erdős-Rényi, Barabasi-Albert, and Watts-Strogatz), while others necessitated some minor variation (stochastic block and tree).

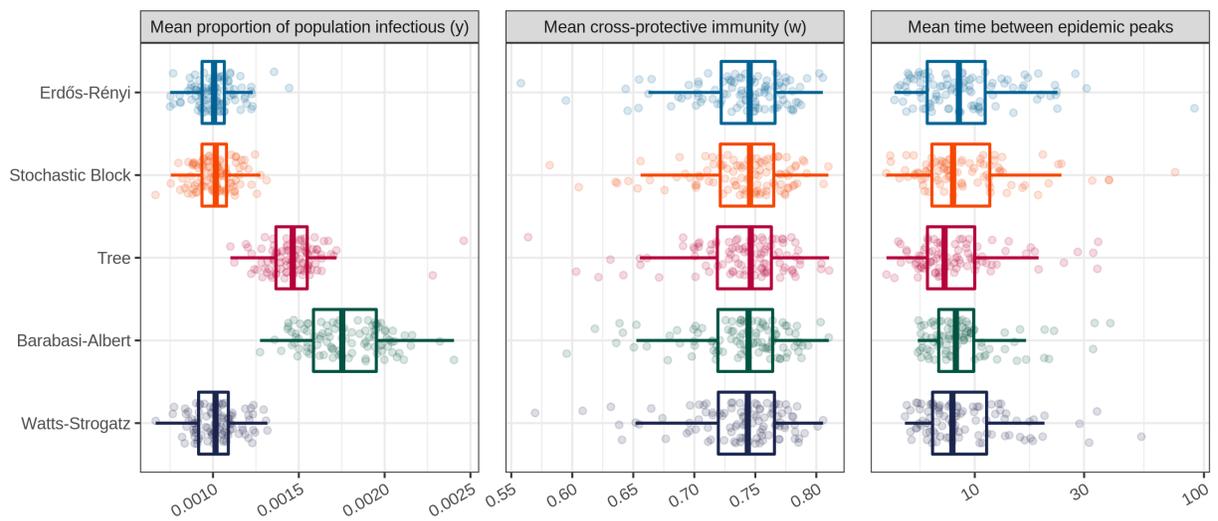


Figure S5: Similar to the lower row of Fig 4, but with γ and σ equal to 0.55 and 32, respectively. All other parameters are equal to or set randomly as in Fig 4. While the observed differences in total infected are robust, note that here the mean time between epidemic peaks is approximately equal across randomizations.